Theoret. chim. Acta (Berl.) 28, 313-337 (1973) 9 by Springer-Verlag 1973

## *Commentationes*

# **A Semiempirical MO Study of the Electronic Structure and Excited States of the** *Tris(2,2'-Bipyridyl)Iron(II)* **and**  *Tris(Glyoxal-Bis-N-Methylimine) Iron(II)I ons*

## Jan Blomquist

Institute of Physics, University of Stockholm, Vanadisvägen 9, 113 46 Stockholm

### Bengt Nordén

Dept. of Inorganic Chemistry, University of Lund, Box 740, 220 07 Lund

## Marianne Sundbom

Institute of Theoretical Physics, University of Stockholm, Vanadisvägen 9, 113 46 Stockholm

#### Received May 23, 1972

A semi-empirical SCF-MO method, the PEEL method, has been applied in an investigation of the electronic structure and excited states of two iron compounds,  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup> and  $[Fe(II)-(bipy)<sub>3</sub>]$ <sup>++</sup>.

The electronic absorption spectra have been recorded. The calculations show that it is necessary to account for the trigonal distortion and the covalency in order to explain these spectra quantitatively. M6ssbauer measurements have also been performed. The calculated electronic population of the iron is in accord with Mössbauer isomer shift data, indicating that a realistic electron distribution has been obtained by the PEEL method.

Eine semiempirische SCF-MO-Methode, die PEEL-Methode, wurde zur Untersuchung der Elektronenstruktur sowie von angeregten Zuständen der beiden Eisenverbindungen [Fe(II)-(GMI)<sub>3</sub>]<sup>++</sup> und  $[Fe(II)-(bipy)_3]^{++}$  angewendet.

Die elektronischen Absorptionsspektren wurden aufgenommen. Die Berechnungen zeigen, dab die trigonale Verzerrung und die Kovalenz beriicksichtigt werden miissen, um die Spektren quantitativ zu erklären. Mössbauer-Messungen wurden ebenfalls durchgeführt. Die berechnete Elektronenverteilung am Eisenatom ist in Obereinstimmung mit den Daten der Isomerenverschiebung der M6ssbauer-Messungen, wodurch gezeigt wird, dab mit der PEEL-Methode eine realistische Elektronen-Verteilung erhalten wurde.

Une méthode SCF-MO semi-empirique, la méthode PEEL, a été appliquée à une étude de la structure électronique et des états excités de deux composés ferreux:  $[Fe(II)-(bipy)_3]^{++}$  et  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup>. Les spectres d'absorption électronique ont été enregistrés. Les calculs montrent qu'il est nécessaire de rendre compte de la distorsion trigonale et de la covalence pour expliquer ces spectres quantitativement.

Des mesures de l'effet Mössbauer ont aussi été effectuées. La population électronique calculée du fer est en bon accord avec les données sur le déplacement isomérique de Mössbauer, ce qui indique que la méthode PEEL fournit une distribution électronique réaliste.

### **1. Introduction**

To obtain an understanding of the activity of organic molecules and organometallic complexes it is necessary to know more about their electronic structure. The present investigation is part of a project whose object is molecular orbital (MO)



Fig. 1. The numbering of the AO's of GMI and bipyridyl. Cf. Fig. 2 and text

studies of molecules of biological interest. This study uses the PEEL method, an extended Pariser-Parr-Pople (PPP) method, that has proved to be successful in accounting for many different properties of large organic molecules  $\lceil 1-3 \rceil$  and organic copper complexes [4-7]. It was found worthwhile to extend the method to complexes of other transition elements. In the present paper the semiempirical parameters for iron complexes are presented.

The two propellershaped ions<sup>1</sup>  $[Fe(II)$ - $(bipy)_3$ <sup>++</sup> and  $[Fe(II)$ - $(GMI)_3$ <sup>++</sup> (bipy=2,2'-bipyridyl; *GMI=glyoxal-bis-N-methylimine)* have been used as model compounds for the determination of semiempirical parameters describing the amount of bonding between iron and the nitrogen ligands. These molecules were chosen because they have been extensively investigated by experimental methods. The calculations have been performed for the right-handed optical isomers (cf. Figs. 1 and 2). The present MO study gives information about the electronic distribution within the complexes, especially the effective electronic population on the iron ion, from which a value of the total electronic density at the iron nucleus can be deduced and compared with the experimental value obtained from M6ssbauer isomer shift data. Further, the study permits a discussion of the different types of transitions in the electronic spectra.

Reviews of previous theoretical investigations and experimental findings for  $[Fe(II)-(bipy)_3]^+$  and  $[Fe(II)-(GMI)_3]^+$  can be found in some recent publications [8, 9]. In most discussions of the electronic spectra of these compounds, octahedral symmetry  $(O_h)$  and crystal field theory have been considered adequate for the assignments. The results of the present investigation, however, show that it is necessary to account for the trigonal distortion and the covalency in order to

<sup>&</sup>lt;sup>1</sup> In this paper the convention has been used that Fe(II) stands for ferrous iron, Fe<sup>2+</sup>.



Fig. 2. The propellershaped structure of  $[Fe(II)-(GMI)<sub>3</sub>] <sup>++</sup>$  and  $[Fe(II)-(bipy)<sub>3</sub>] <sup>++</sup>$ . *xyz* denotes the  $D_3$  symmetry adapted right handed coordinate system with z as threefold axis and x through the twofold axis of ligand  $A$ . Cf. Fig. 1 and text

explain these spectra quantitatively. Day and Sanders  $[10, 11]$  discussed the CT band of the similar phenanthroline complex, using Hückel molecular orbitals and a simple treatment of CT states  $[12, 13]$ . In a more elaborate theoretical treatment of these molecules Ito, Tanaka, Hanazaki and Nagakura [14-16] were able to give a more quantitative discussion of the electronic transitions. They used an extension of the "molecules-in-molecule" method  $[13, 16]$  for their studies of metal complex ions, considered explicitly  $\pi$  orbitals of the ligands and d orbitals of the iron ion, and used locally excited ligand transitions together with electron transfer  $(d \rightarrow \pi^*)$  transitions in their CI-treatment. Thus their methods did not allow for a discussion of transitions of  $(d \rightarrow d)$  type.

In the present investigation 4s and 4p orbitals have been included, and the energy levels of excited states have been calculated by mixing all types of configurations obtained from single excitations. The theoretical model is discussed in Sections 3 and 4.

The electronic absorption spectra have been investigated experimentally and M6ssbauer measurements have also been performed.

### **2. Experimental**

*~'is-(2,2'-bipyridyl) iron(II) sulphate* was prepared according to a method of Jaeger and van Dijk [17]. The precipitate was washed with ether and dried over  $P_2O_5$  for one week. It corresponded to a composition  $Fe(bipy)_3 \cdot SO_4 \cdot 5H_2O$ .

*(Analysis:* C 50.7, H 4.7, S 5, N 11.9; Calc. for  $\text{FeC}_{30}N_6H_{24}SO_4.5H_2$ . C 50.7, H 4.8, S 4.5, N 11.8.)

*Tris-(glyoxal-bis-N-methylimine) iron(II)iodide* was obtained in the way described by Krumholz [18] and dried over  $P_2O_5$  for one week.

*(Analysis: C* 26.0, H 5.1, N 15.0; calculated for  $\text{FeC}_{12}N_6H_{24}I_2$ : C 25.6, H 4.3, N 14.9.)

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*The UV spectra* in the range 15-54 kK were recorded on  $10^{-4}$  M solutions (aqueous for the GMI complex, and methanolic for the bipyridyl complex) with a Cary 15 recording spectrophotometer. Spectrograde methanol was used without further purification. In the 10 kK range a Hitachi EPS-3T spectrophotometer was used on 0.3 M aqueous solutions. Concerning the iodide, it was carefully checked that no photolysis intervened. The UV spectrum could be exactly reproduced in several runs. The results are given in Tables 6, 7, 10 and 11 and Figs. 3 and 4.



Fig. 3. The electronic absorption spectra of  $[Fe(II)-(GMI)<sub>3</sub>]$ .  $I<sub>2</sub>$  in aqueous solution (----), and of  $[Fe(II)–(bipy)_3] \cdot SO_4 \cdot 5H_2O$  in methanol (----). The visible region



Fig. 4. The electronic absorption spectra of  $[Fe(II)-(GMI)<sub>3</sub>]$ .  $I<sub>2</sub>$  in aqueous solution (- $[Fe(II)–(bipy)_{3}] \cdot SO_{4} \cdot 5H_{2}O$  in methanol (-----). The UV region -), and of

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*Mdssbauer spectra* were measured at room temperature with an electromechanical transducer of Kankeleit type in combination with an Intertechnique 400-channel analyser and a Hilger and Watts P 1028 scintillation detector. The source was  $5 \text{ mC}^5$ <sup>7</sup>Co in Pd foil kept at the same temperature as the absorber. The velocity was calibrated using the magnetic splitting of natural iron. The Mössbauer lines were fitted to Lorentzians by means of a least squares method. Also in this case the spectra were satisfactorily reproduced in several runs with different samples. The results are given in Table 5.

More details about the Mössbauer study can be found in Ref. [47].

### **3. Theoretical Model**

In applying the methods of quantum chemistry to large molecular systems, approximations must be made to simplify the work required and reduce the amount of computertime utilized drastically. Roos and Skancke [19] suggested a new scheme for the evaluation of semiempirical parameters in a modified PPPmethod for  $\pi$  systems. In order to allow for a systematic study of large organic molecules, this scheme has been extended. The method is now applicable to the  $\pi$ -electron system of various heteroaromatic systems and to  $\sigma$  lone pair electrons  $(n)$  for nitrogen-containing molecules (see [3] for references). An extension of the PPP-method to organometallic molecules was suggested by Roos [4]. This method has been applied to Cu complexes  $[4-7]$  and has given very promising results. In the present work the scheme is extended to include iron complexes. The method has been thoroughly presented previously [4, 7] and will only be shortly outlined here:

1. The method is based on the Roothaan MO-SCF method for open shell systems [20].

2. The electrons have been divided into two groups, the core and the peel. The core group is not explicitly taken into account; it merely contributes a constant charge density, corresponding to a fixed electrostatic potential field. The Hamiltonian of the peel electrons can be written:

$$
H = \sum_{i} H_{(i)}^{\text{core}} + \sum_{i < j} 1/r_{ij} \tag{1}
$$

where  $H_{(i)}^{\text{core}}$  is the sum of the kinetic and potential energy operator for electron i. The peel consists of the valence electrons of the metal atom, the ligand lone-pair electrons, and the  $\pi$  electrons of the ligands. The molecular orbitals are given as linear combinations of atomic orbitals, which are taken to be:  $3d$ , 4s and 4p orbitals on the metal atom,  $\sigma$  lone-pair orbitals for the ligand atoms, and one  $\pi$  orbital for each of the atoms contributing  $\pi$ -electrons to the system.

3. The zero differential overlap (ZDO) approximation is applied to all twoelectron integrals except for the one-center exchange integrals.

4. Only resonance integrals between neighbouring atoms are retained, in correspondance with the nature of the ZDO approximation.

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5. The method is semi-empirical. The following integrals are determined from atomic or molecular ionization potentials and spectral data:

Resonance integrals,  $\beta_{\mu\nu} = H^{\text{core}}_{\mu\nu}$  ( $\mu$  and  $\nu$  neighbours),

two-center coulomb integrals,  $\gamma_{uv}$  ( $\mu$  and  $\nu$  neighbours),

one-center coulomb integrals,  $J_{\mu\nu}$ ,

one-center exchange integrals,  $K_{uv}$ ,

parts of the one-center core integrals,  $\alpha_{\mu} = H_{\mu\mu}^{\text{core}}$ .

 $\alpha_{\mu}$  is decomposed according to a technique due to Goeppert-Mayer and Sklar [22], and described further in next section.

6. Excited states are calculated by means of the method of superposition of configurations. All types of singly excited configuration are included.

### **4. Semiempirical Iron Parameters**

The extended PPP-method can be formulated in terms of two types of integrals: one-electron integrals occurring in the core matrix  $H<sup>core</sup>$ , and two-electron integrals of coulomb and exchange type. In a semiempirical theory these integrals should be expressible in terms of a limited set of semiempirical parameters. The idea is to determine as many as possible of these parameters from experimental data. A general scheme using experimental data has been developed for the evaluation of semiempirical parameters of carbon and hetero atoms (see [3] for further references). In the present work previously determined carbon and nitrogen parameters [1, 3] have been used.

Semiempirical parameters for the iron atom and for the iron ligand bond have been derived in the present work and will be discussed in detail. It should be stressed that the procedure to obtain these parameters necessarily must be more uncertain depending on the greater complexity, e.g. the metal atom contributes nine AO's to the basis set, and the lack of sufficient experimental information.

## *Two-Electron Integrals*

1. One-center coulomb,  $J_{\mu\nu}$ , and exchange,  $K_{\mu\nu}$ , integrals are considered and expressed in terms of Slater-Condon parameters  $F_k$  and  $G_k$  [40, 41]. These parameters were determined from iron atomic spectra and atomic Hartree-Fock calculations (see Appendix 1). They are considered dependent on charge,  $q$ , or number of *d*-electrons,  $n_a$ . Values obtained are given in Table 1.

2. Of the two-center two-electron integrals only the coulomb integrals,  $\gamma_{\mu\nu}$ , are retained. They were calculated by means of an interpolation formula suggested by Roos [4, 21]:

$$
\gamma_{\mu\nu}(R) = \frac{1}{2}(\gamma_{\mu\mu} + \gamma_{\nu\nu}) \cdot f(z) \tag{2}
$$

where  *is the distance between the orbitals,* 

$$
z = \frac{1}{2}(\gamma_{\mu\mu} + \gamma_{\nu\nu})R
$$
 (3a)

and 
$$
f(z) = 1/(z + e^{-z}).
$$
 (3b)

Formula (2) is independent of the orientation of local coordinate axes.

	$q^{\rm b}$			
	$q = 0$	$q = +1$	$q = +2$	
$\rm{SCP}^a$				
	$-490.37$	$-560.95$	$-612.78$	
$\varepsilon_{\rm s}$	49.70	58.29		
$F_0$ (ss)			84.06	
$F_0(sd)$	62.17	73.12		
$G_2(sd)$	1.290	1.560	1.830	
$\varepsilon_p$	$-356.83$	$-449.38$	$-481.79$	
$F_0(pp)$	43.74	55.24		
$F_2(pp)$	0.919	1.160		
$F_0(sp)$	46.72	56.77		
$G_1(sp)$	10.023	12.573		
$G_1(pd)$	0.324	0.478	0.632	
$G_3(pd)$	0.0162	0.0239	0.0316	
$F_0(pd)$	46.66	61.42	68.47	
$F_2(pd)$	0.275	0.351	0.411	
	$n_d^{\text{c}}$			
	$n_a=8$	$n_d = 7$	$n_d = 6$	$n_d = 5$
SCP				
$\varepsilon_{\scriptscriptstyle A}$	— 734.40	$-767.93$	$-793.83$	$-808.48$
$F_0(dd)$	95.89	105.54	115.19	124.84
$F_2(dd)$	1.075	1.246	1.418	1.589
$F_4(dd)$	0.096	0.105	0.114	0.123

**Table 1. One-center semiempirical parameters (in kK) for** Fe

<sup>a</sup> SCP stands for Slater-Condon parameter.

b q **is the charge of the iron ion.** 

 $n_d$  is the number of 3d electrons of the iron ion.

### *One-Electron Integrals*

The one-electron operator  $H^{\text{core}}$  has the following form:

$$
H^{\text{core}} = T + U^{\text{core}}(\text{Me}) + \sum_{i} U^{\text{core}}(L_i)
$$
 (4)

where  $T$  denotes the kinetic energy operator,  $U^{\text{core}}(Me)$  the potential field from the metal core and  $U^{\text{core}}(L_i)$  the corresponding field from the ligand atom *i*.

1. The core integral  $\alpha_{\mu}$ , where  $\mu$  is a metal atomic orbital, can be decomposed **in the following way:** 

$$
\alpha_{\mu} = \varepsilon_{\mu} - \sum_{i} \sum_{\nu(i)} n_{\nu(i)} \gamma_{\mu\nu(i)} + \Delta \alpha_{\mu}
$$
 (5)

**where** 

$$
\varepsilon_{\mu} = \langle \mu | T + U^{\text{core}}(\text{Me}) | \mu \rangle \tag{6}
$$

**and** 

$$
\Delta \alpha_u = \Sigma \langle \mu | U^0(L_i) | \mu \rangle \,. \tag{7}
$$

This technique to rewrite  $\alpha_{\mu}$  is due to Goeppert-Mayer and Sklar [22].  $\varepsilon_{\mu}$  contains **the interaction between a metal electron and the metal core. The matrix elements,**   $\varepsilon_{\mu}$ , were determined from atomic ionization potentials and atomic spectral data (see Appendix 1 and Table 1). In the second part of (5)  $n_{v(i)}$  is the number of electrons

associated with the atomic orbital  $v(i)$  at the ligand atom i.  $\Delta \alpha_u$  represents the penetration between a metal orbital and a neutral atom and was roughly estimated as follows: The nitrogen atoms were treated as point dipoles (in the center of the nitrogen atom) with a dipole moment of 2.25 D corresponding to the dipole moment of pyridine [23] and with a direction opposite to the vector connecting the center of the nitrogen atom to the center of charge of the  $sp^2$ -hybridized lone pair of nitrogen.  $\Delta \alpha_n$  was estimated as the interaction between these dipoles and an electronic charge situated at the center of charge of the orbital  $\mu$ . This method gave a value of 0.367 a.u. for the bipy complex and a value of 0.359 a.u. for the GMI complex. In this context it should be noted that it would be desirable to consider the sum of the first and third terms of (5) as one parameter to be determined from experimental data; e.g., ionization potentials of a series of similar iron complexes, thus applying a method similar to the one used for  $\pi$  systems. Unfortunately the lack of experimental data confines us to use the present much cruder method.

The core integrals  $\alpha_{v_{\text{c}}(\pi)}$ ,  $\alpha_{v_{\text{N}}(\pi)}$ , and  $\alpha_{v_{\text{N}}(\pi)}$ , where  $v_{\text{c}}(\pi)$ ,  $v_{\text{N}}(\pi)$  and  $v_{\text{N}}(n)$  are ligand atomic orbitals, are also decomposed according to the Goeppert-Mayer and Sklar method:

$$
\alpha_{v_{\mathcal{C}}(\pi)} = W_{v_{\mathcal{C}}(\pi)} - \sum_{v' \neq v_{\mathcal{C}}(\pi)} n_{v'} \gamma_{v'v_{\mathcal{C}}(\pi)} - \sum_{\mu} n_{\mu} \gamma_{\mu v_{\mathcal{C}}(\pi)} + \langle v_{\mathcal{C}}(\pi) | U^{0}(\mathbf{M}e) | v_{\mathcal{C}}(\pi) \rangle ; \tag{8}
$$

$$
\alpha_{\nu_{N}(\pi)} = W_{\nu_{N}(\pi)} - 2J_{\nu_{N}(\pi)\nu_{N}(n)} + K_{\nu_{N}(\pi)\nu_{N}(n)} - \sum_{\nu' \neq {\nu_{N}(\pi) \text{ and } \nu_{N}(n)}} n_{\nu'} \gamma_{\nu'\nu_{N}(\pi)} - \sum_{\mu} n_{\mu} \gamma_{\mu\nu_{N}(\pi)} + \langle \nu_{N}(\pi)| U^{0}(\text{Me}) | \nu_{N}(\pi) \rangle ;
$$
\n(9)

$$
\alpha_{\nu_{N}(n)} = W_{\nu_{N}(n)} - J_{\nu_{N}(\pi)\nu_{N}(n)} + \frac{1}{2} K_{\nu_{N}(\pi)\nu_{N}(n)} \n- \sum_{\nu' \neq (\nu_{N}(\pi) \text{ and } \nu_{N}(n)} - \sum_{\mu} n_{\mu} \gamma_{\mu\nu_{N}(n)} + \langle \nu_{N}(n) | U^{0}(\text{Me}) | \nu_{N}(n) \rangle ;
$$
\n(10)

 $v'$  denotes a ligand atomic orbital and  $\mu$  a metal atomic orbital. In the present work the terms expressing the ligand metal penetration,  $\langle v|U^0(Me)|v\rangle$ , have been neglected as was also done in previous calculations on copper complexes. The parameters  $W<sub>v</sub>$  are discussed in detail in previous papers [1, 3, 19].

2. The formula of Wolfsberg and Helmholtz [24] was used for the resonance

$$
\beta_{\mu\nu} = -\frac{k_{\mu}}{2} \cdot S_{\mu\nu}(I_{\mu} + I_{\nu})
$$
\n(11)

where  $\mu$  is a metal orbital (3d, 4s, or 4p) and v an orbital of the nitrogen atoms.

Here  $I_u$  and  $I_v$  are valence state ionization potentials,  $S_{uv}$  the overlap integral between  $\mu$  and v, and  $k_{\mu}$  constants to be determined from molecular spectral data<sup>2</sup>. The overlap integrals were calculated theoretically from atomic Hartree-Fock orbitals for iron [25, 26] and nitrogen [26]. In line with previous studies on copper complexes, the preliminary intention was to investigate whether three different values,  $k_{3d}$ ,  $k_{4s}$ , and  $k_{4m}$ , could be determined from the electronic spectral data of the bipyridyl and GMI complexes of iron(II). The initial values for these parameters were taken from previous studies of copper complexes [4, 5]. The calculated

<sup>&</sup>lt;sup>2</sup> The assumed occupation numbers in determining the metal  $I_{\mu}$  values are  $3d^6$ 4s4p for 4p and  $3d^6$  4s<sup>2</sup> for 4s and 3d.

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spectra were found to be predominantly determined by the value of  $k_{3d}$ . A satisfactory agreement between theory and experiment was obtaines for  $k_{3d} = 3.26$  and  $k_{4s} = k_{4p} = 1.0$ . It should be noted, however, that the calculated spectra are insensitive to moderate changes in  $k_{4s}$  and  $k_{4p}$ .

### **5. Details of the Calculation**

As far as we know there are no X-ray diffraction data for the iron(II) complexes with *tris-(2,2'-bipy)* and *tris-(GMI).* From an analysis of measured NMR spectra of  $[Fe(II)-(dipy)_{3}]Cl_{2}$  Castellano, Günther and Ebersole [27] concluded that the *cis-planar* conformation of the bipyridyl groups was in line with the measured values of the chemical shifts. They also derived a metal-nitrogen distance of 2 A. For a similar complex, *tris-o-phenanthroline* iron(II), Templeton, Zalkin and Ueki  $\lceil 28 \rceil$  obtained an average iron-nitrogen distance of 1.97 Å. In the present calculations of the two diamagnetic complexes  $[Fe(II)-(bipy)]$ <sup>++</sup> and  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup> the Fe-N distance is assumed to be 2.0 Å. This is also in accord with recent X-ray data on a high-spin and a low-spin form of  $F_{\rm}$ e(dipy)<sub>2</sub>(NCS)<sub>2</sub> by König and Watson [29]. They obtained an average Fe-N distance of about  $2.02 \text{ Å}$  for the low spin (singlet) form. Both complexes are assumed to have  $D_3$  symmetry. The dipyridyl ligands are assumed to have *cis*planar structure with the same interatomic distances as found from electron diffraction measurements [30]. This structure was also used in a previous MO calculation [31] on the planar *cis-* and *trans-forms* of bipyridyl.

There are no experimental structural data of GMI. A first separate MO calculation was performed for GMI with the same reasonable assumption of geometry as was made by Ito et al. [14] in their theoretical investigation of GMI and the *tris*-(GMI) iron(II) complex. New bond distances were obtained from the calculated bond orders,  $p_{uv}$ , by means of the relations [1, 19]

$$
R_{\mu\nu}(C, C) = 1.517 - 0.18 p_{\mu\nu}, \qquad (12)
$$

$$
R_{\mu\nu}(C, N) = 1.458 - 0.18 p_{\mu\nu}.
$$
 (13)

The calculation on GMI was repeated with the obtained bond distances and with angles for GMI such that in the iron complex the N-Fe-N angle would be  $90^\circ$ for the Fe-N distance equal to 2.0 A. The structures of GMI and dipy are shown in Fig. 1 and the interatomic distances used in the calculations are given in Table 2.

Table 2. Bond distances (in A) for GMI and bipyridyl chosen for the calculations. The numbering of the atoms are given in Fig. 1 and in text (Section 5)

<b>GMI</b>		Bipyridyl					
Bond	Bond length	Bond	Bond length				
$4 - 1$	1.4600	$4 - 1$	1.4700				
$7 - 1$	1.2878	$7 - 1:13 - 7$	1.3394				
$Fe-N$	2.0000	$19 - 13:31 - 1$	1.3958				
		$25 - 19$ ; $31 - 25$	1.3936				
		$Fe-N$	2.0000				

Both in the calculation of GMI and  $(Fe(II)-(GMI)<sub>3</sub>)$ <sup>++</sup> the influence of the CH<sub>3</sub> groups was neglected.

The propellershaped structure of the complexes is visualized in Fig. 2, where the three ligands are denoted A, B and C. The calculations were performed for the right-handed optical isomers  $\lceil 32 \rceil$ .

In the following, x, y, z denotes the coordinate system adopted to  $D_3$  symmetry. The z-axis is taken as the threefold symmetry axis, and the x- and  $\nu$ -axes are taken to form a right-handed system with the positive x-axis passing through the twofold axis of ligand A (cf. Fig. 2),

$$
\hat{x} = \frac{1}{\sqrt{2}} (\hat{\xi} - \hat{\eta})
$$
\n
$$
\hat{y} = \frac{1}{\sqrt{2}} (\hat{\xi} + \hat{\eta} - 2\hat{\zeta})
$$
\n
$$
\hat{z} = \frac{1}{\sqrt{2}} (\hat{\xi} + \hat{\eta} + \hat{\zeta}).
$$
\n(14)

This same choice of axes was also made by Day and Sanders [11].

The numbering of the atomic orbitals in ligand A is given in Fig. 1. If  $i$  numbers an AO on ligand A,  $(i + 1)$  will number the corresponding AO on ligand B, and  $(i + 2)$  the corresponding AO on ligand C.

The atomic orbitals that constitute the basis for the calculations are 27 for the GMI complex and 51 for the dipy complex: the 3d, 4s and 4p orbitals of the iron ion, one  $sp^2$  hybridized lone pair orbital (n) from each nitrogen, and one  $\pi$ orbital from each of the carbon and nitrogen atoms of the ligands. For the GMIcomplex the atomic orbitals with numbers from 1-12 refer to ligand  $\pi$  orbitals, while for the dipy complex,  $1-36$  refer to  $\pi$  orbitals. The number of electrons taken into account is 30 in the GMI complex and 54 in the dipy complex; in each complex, 6 electrons come from the iron ion and the rest from the ligands.

The self-consistent field molecular orbitals were evaluated by means of a computer program, SCF-OPSZDO, written by B. Roos and M. Sundbom. This program also calculates the energy levels of excited states by mixing configurations from single excitations. All computations were made on an IBM 360/75 computer. The program and the computer limit the number of configurations for each symmetry to 140. Thus for the bipy complex not all of the single excitations could be considered. The CI treatment was restricted for each symmetry to 140 configurations.

The values of the one-center semiempirical parameters of iron depend on the electronic population of the iron ion (see appendix). A reasonable guess of the electronic population was made from Mössbauer isomer shift data, according to a method presented in a previous publication [33]. The initial effective configuration of the iron ion was thus guessed to be  $(3d)^{5.75}$   $(4s)^{0.5}$ . The values of the onecenter parameters for this configuration were obtained by interpolation in Table 1 and were used in the preliminary calculations to obtain reasonable values of the parameters  $k_{\mu}$ , which occur in the expressions for the resonance integrals (cf. Section 3). When reasonable values for  $k_{\mu}$  had been obtained, new one-center iron **parameters were determined from the calculated effective configuration. The whole calculation was repeated with these new parameters. This procedure was repeated until self-consistency was achieved. In view of the simplified electron configuration dependence of the one center iron parameters (see appendix) the**  calculation was repeated only if the calculated values of  $n_{3d}$  and q deviated from the input values by more than  $\pm 0.1$ . This selfconsistency in charge procedure was then repeated for each set of trial  $k_{\mu}$  values.

### **6. Molecular Orbitals and Ground State Properties**

The SCF molecular orbitals and eigenvalues of  $[Fe(II) – (GMI)<sub>3</sub>]<sup>++</sup>$  are **presented in Tables 3 and 4. The orbital pattern is similar for both compounds.** 

## $[Fe(II)–(GMI)<sub>3</sub>]<sup>++</sup>$

**From Table 4 where the total electron population of the atomic orbitals is**  given, the configuration of the Fe ion is found to be  $(3d)^{5.46} (4s)^{0.42} (4p)^{0.42}$  with **a net charge of + 1.70 on iron. The Table 4 contains a comparison with the elec-**

MO <sup>a</sup>				The electron population <sup>b,c</sup>							
No.	Sym- metry	$\varepsilon_i$	$C_{1}$	N,	$n_{\tau}$	$z^2$	$xy + (x^2 - y^2)$	$xz + yz$ s		$x + y z$	
1	$1a_1$	$-1.0887$	0.000	0.000	0.131	0.004	$\theta$	$\Omega$	0.209	$\Omega$	$\Omega$
2:3	1e	$-1.0706$	0.000	0.000	0.260	$\Omega$	0.147	0.292	$\theta$	0.001	$\overline{0}$
4	1a <sub>2</sub>	$-0.9736$	0.001	0.003	0.150	$\Omega$	$\theta$	$\Omega$	$\theta$	$\bf{0}$	0.079
5;6	2e	$-0.9642$	0.004	0.013	0.290	$\Omega$	0.019	0.013	$\bf{0}$	$0.126$ 0	
7:8	3e	$-0.8801$	0.094	0.179	0.023	$\Omega$	0.155	0.062	$\bf{0}$	0.001	$\theta$
9	$2a_1$	$-0.8597$	0.014	0.090	0.000	0.372	$\mathbf 0$	$\mathbf{0}$	0.002	$\Omega$	$\theta$
10	$2a_2$	$-0.8542$	0.075	0.087	0.004	$\Omega$	0	$\mathbf 0$	0	$\Omega$	0.002
11:12	4e	$-0.8027$	0.072	0.249	0.000	$\Omega$	0.050	0.019	$\theta$	0.001	$\Omega$
13	$3a_1$	$-0.6774$	0.027	0.039	0.000	0.598	$\Omega$	$\bf{0}$	0.002	$\Omega$	0
14;15	5e	$-0.6567$	0.141	0.024	0.001	$\Omega$	0.754	0.245	0	$0.000 \quad 0$	
16	$3a_2$	$-0.4066$	0.091	0.073	0.001	$\Omega$	$\Omega$	$\theta$	$\mathbf 0$	$\theta$	0.011
17:18	6e	$-0.3407$	0.100	0.121	0.001	$\Omega$	0.507	0.120	$\theta$	$0.038$ 0	
19:20	7e	$-0.2539$	0.254	0.070	0.000	$\theta$	0.052	0.003	0	$0.001$ 0	
21	4a <sub>1</sub>	$-0.2490$	0.126	0.037	0.000	0.025	$\Omega$	$\theta$	0.000	$\mathbf{0}$	$\theta$
22;23	8e	$-0.1818$	0.001	0.001	0.072	$\theta$	0.314	1.246	$\theta$	$0.000 \& 0$	
24	$5a_1$	$-0.0964$	0.000	0.000	0.035	0.001	0	$\bf{0}$	0.788	$\theta$	$\theta$
25,26	9е	0.0107	0.001	0.008	0.018	$\Omega$	0.002	0.000	$\Omega$	$1.831$ 0	
27	$4a_2$	0.0252	0.000	0.003	0.012	$\theta$	$\mathbf{0}$	$\bf{0}$	$\theta$	$\bf{0}$	0.908

Table 3. Molecular orbitals of  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup>. Orbital energies  $\varepsilon$ , in a.u. The electronic population. **The numbering system as in Fig.** 1

<sup>a</sup> The 15 lowest orbitals are doubly occupied.

**b Formal population of the virtual orbitals.** 

 $\epsilon$  For orbitals of e symmetry the sum of population for  $e_x$  and  $e_y$  is given.

 $N_7$  and  $C_1$  denotes  $\pi$  orbitals on nitrogen and carbon,  $n_7$  denotes a nitrogen  $\sigma$  lone pair orbital.  $z^2$  stands for  $3d_{z^2}$ , s for 4s and x for  $4p_x$  on iron.

AO	$[Fe(II)–(GMI)3]++$	GMI(cis)	$GMI$ (trans)	
GMI:				
C	0.856	0.981	0.979	
N	1.372	1.019	1.021	
n	1.721	2.000	2.000	
Fe:				
$z^2$	1.947			
$x^2 - y^2$ ; xy	1.124	$n_{3d} = 5.457$		
yz; xz	0.631			
s	0.424		$q = 1.701$	
x; y	0.128	$n_{4s} = 0.424$ $n_{4p} = 0.418$		
z	0.162			

Table 4. The electronic population of the atomic orbitals in [Fe(II)-(GMI)<sub>3</sub>]<sup>++</sup>, GMI *(cis)* and GMI *(trans)* 

tronic population in GMI. Further, this table shows that there is a synergic interaction between metal-ligand  $\sigma$ - and  $\pi$ -bonding, resulting in a net transfer of electrons from the ligand  $\sigma$  system to mainly the 4s, 4p and 3d orbitals of Fe and in a backdonation from the 3d orbitals to the ligand  $\pi$  system.

The value of the electronic density at the iron nucleus,  $|\psi(0)|^2$ , deduced from the calculated effective configuration of valence electrons by a recently published method [33], is in good agreement with the value obtained from the measured M6ssbauer isomer shift (Table 5).

As shown in Table 3 the molecular orbital  $1a_1$  is mainly a ligand nitrogen lone pair orbital, stabilized by bonding to Fe 4s (21%).  $2a_1$  is a bonding and  $3a_1$  an antibonding metal-ligand ( $\pi$ ) orbital with 37% and 60%  $d_{\pi^2}$ -character respectively. The orbital 1a, is a ligand n orbital weakly stabilized by  $4p_7$  (8%), while  $2a_2$  can be considered as a pure ligand  $\pi$  orbital. As shown in Table 3 1e is mainly a ligand n-orbital (22% d-character),  $2e$  is a ligand n orbital, while  $3e$  and  $4e$  are ligand  $\pi$  orbitals. 5e has 50% metallic 3d and 50% ligand  $\pi$  character.

The results of the present MO study show that only one orbital  $(3a_1)$  is mainly (60%) metallic, indicating the difficulty in discussing this compound from the crystal field point of view. In many previous discussions the splitting of the octahedral levels have been considered small and generally neglected. This assumption is not justified by the present results.

## $[Fe(II)–(bipy)_3]^{+ +}$

The orbital pattern resembles that of the GMI complex.

The configuration of the Fe ion is found to be  $(3d)^{5.47} (4s)^{0.42} (4p)^{0.42}$  with a net charge of 1.69 on iron. As shown in Table 5, the calculated effective electronic configuration yields a value of the electronic density at the nucleus in accord with the value obtained from the observed Mössbauer isomer shift. The good agreement

	Calcula-	<b>Observations</b>							
	tion	Epstein [34]			Present work				
	$ \psi(0) ^2$	$\delta^a$ (mm/s) at $300^\circ$ K	$ \psi(0) ^2$	$\delta^a$ (mm/s) at $80^\circ$ K	$  \psi(0)  ^2$	$\delta^a$ (mm/s) at $300^\circ$ K	$  \psi(0)  ^2$		
$[Fe(II)–(GMI)3]++$	11907.75	0.414 $+0.010^{\circ}$	11907.53	0.515 $+0.04 + 0.013$ <sup>b</sup>	11907.17	0.27 $+0.04 +0.01$ <sup>c</sup>	11908.04 $\pm 0.04$		
$[Fe(II)–(bipy)]^{-+}$	11907.66	0.367 $+0.008b$	11907.70	0.403 $+0.03 + 0.005^{\circ}$	11907.57	0.41 $+0.02 + 0.01$ <sup>d</sup>	11907.55 $+0.04$		

Table 5. The electron density at the Fe nucleus,  $|\psi(0)|^2$ , for  $[Fe(II)-(GMI)_3]^{++}$  and  $[Fe(II)-(bipy)_3]^{++}$ . Calculated values compared with values derived from experimental Mössbauer isomer shifts,  $\delta$  [33]

<sup>a</sup> Relative stainless steel (SS). (Add 0.161 mm/s to convert to sodium nitroprusside as references substance.)

**b** The perchlorate salts.

 $\text{Fe}$  Fe-(GMI)<sub>3</sub>I<sub>2</sub>.

 $^{\text{d}}$  Fe-(bipy)<sub>3</sub>  $\cdot$  SO<sub>4</sub>  $\cdot$  5H<sub>2</sub>O.

between theoretical and experimental values indicates that the present MO method can be used with some confidence for the determination of the electronic distribution in transition metal complexes.

The orbital pattern shows that  $O<sub>h</sub>$  symmetry will not be adequate for the assignment of electronic transitions. Distortions due to the actual  $D_3$  symmetry are considerable and cannot be neglected. Furthermore no orbital can be considered as purely metallic, thus indicating that crystal field theory cannot be used to give a realistic picture of the electronic energy levels.

## **7. Excited States**

The present CI treatment allows a quantitative description of the excited electronic energy levels. The calculations show that it is possible to classify only a few of the excited states as pure  $d-d$ ,  $\pi-\pi^*(L)$ , or CT transitions. This was also found in previous calculations on organic copper complexes [4-7]. The results are presented in Tables 6-12. For comparison the spectra of planar *cis*and *trans-forms* of GMI and bipyridyl have also been calculated (for bipyridyl, see Ref. [31]). The values obtained are given together with experimental data in Table 12.

## $[Fe(II)–(GMI)<sub>3</sub>$ <sup>++</sup>

Most transitions can be classified as partly  $CT$  and partly  $L$ . The observed intense visible band at 18 kK is assigned to the  $3^{1}E$  state (calc. 19.9 kK), which is mainly a combination of the configurations (5e $\rightarrow$ 6e) and (5e $\rightarrow$ 3a<sub>2</sub>) (Table 8). They both have some  $d \rightarrow \pi^*$  character. The amount of electron transfer is 0.25, as shown in Table 9, where the electronic populations for some of the excited states are given.

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Type <sup>a</sup>	Symmetry	Calculated		Observed					
				Ito et al. $[14]$ <sup>b</sup>		Present investigation			
		ν	$\int$	$v_{\rm max}$	$\log \varepsilon_{\rm max}$	$v_{\rm max}$	Range	$\log \varepsilon_{\rm max}$	
$CT + L$	$1^1A_2$	14.1	0.0003						
$CT + d - d$	$1^1E$	14.3	0.00003						
CT	$2^1A_2$	15.2	0.004						
$CT + L$	$2^1E$	15.3	0.004						
$CT + L$	$3^1E$	19.9	0.38	18.5	3.9	18.0		3.94	
$d-d$	$4^1E$	21.8	0.0008	19.4 <sup>s</sup>	3.8	19.8 <sup>s</sup>	$17 - 22$	3.79	
$CT + d - d$	$5^1E$	30.9	0.03	29.1	2.3			28.5–29.4 very weak	
$CT + d - d$	$3^{1}A_{2}$	31.0	0.0004						
$CT + d - d$	$1^1A_1$	32.3	0						
$CT + L$	$2^1A_1$	37.3	0						
$CT+L$	$4^{1}A_{2}$	48.4	0.17	45.0 <sup>s</sup>	4.0	44.3	$42 - 47.5$	4.55	
$CT + L$	$6^1E$	48.5	0.01						
$CT + L$	$7^1E$	50.4	0.05						
$CT+L$	$8^1E$	50.6	0.21						
$CT + L$	$3^{1}A_{1}$	50.9	$\bf{0}$						
$CT + L$	$9^1E$	51.5	0.16						
$CT + L$	$4^{1}A_1$	55.1	$\bf{0}$						
L	$10^1E$	59.9	0.03						
$CT + L$	$5^{1}A_{2}$	60.2	0.40	54.7	4.6	54	$47.5 \rightarrow 54$ 4.8		

Table 6. Electronic singlet transitions in  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup>. Transition frequencies in kK

<sup>a</sup> CT = charge transfer;  $L$  = intraligand  $\pi - \pi^*$ .

*b tris(glyoxal-bis-N-methylimine)iron(II)* tetrafluoroborate in an aqueous solution. The values are estimated from Fig. 1 in [14b].





a Observed. See Table 6.

<sup>b</sup> Ito *et al.* [14] observed a shoulder band near 25 kK, that may be assigned to one or all of the three triplets:  $3<sup>3</sup>A<sub>2</sub>$ ,  $5<sup>3</sup>E$  and  $2<sup>3</sup>A<sub>1</sub>$ .

Symmetry	Wave function
$1^3A_1$	$0.96(5e \rightarrow 6e)^T$
$1^3E$	$-0.62$ (5e $\rightarrow$ 6e ) <sup>T</sup> + 0.25 (3a <sub>1</sub> $\rightarrow$ 6e ) <sup>T</sup> + 0.72 (5e $\rightarrow$ 3a <sub>2</sub> ) <sup>T</sup>
$2^3E$	0.45 (5e $\rightarrow$ 6e ) <sup>T</sup> + 0.83 (3a <sub>1</sub> $\rightarrow$ 6e ) <sup>T</sup>
$1^3A_2$	$0.52 (5e \rightarrow 6e)^{T} + 0.81 (3a_1 \rightarrow 3a_2)^{T}$
$3^3E$	0.59 (5e $\rightarrow$ 6e ) <sup>T</sup> – 0.38 (3a <sub>1</sub> $\rightarrow$ 6e ) <sup>T</sup> + 0.66 (5e $\rightarrow$ 3a <sub>2</sub> ) <sup>T</sup>
$4^3E$	$0.92 (3a_1 \rightarrow 8e)$ <sup>T</sup> + 0.39 $(2a_1 \rightarrow 8e)$ <sup>T</sup>
$1^1A_2$	0.98 (5e $\rightarrow$ 6e ) <sup>S</sup>
$2^{3}A_{2}$	$0.82 (5e \rightarrow 6e)^{T} - 0.51 (3a_1 \rightarrow 3a_2)^{T}$
$1^1E$	0.28 (5e $\rightarrow$ 6e ) <sup>S</sup> + 0.91 (3a <sub>1</sub> $\rightarrow$ 6e ) <sup>S</sup> - 0.23 (2a <sub>1</sub> $\rightarrow$ 6e) <sup>S</sup>
$2^1A_2$	0.99 $(3a_1 \rightarrow 3a_2)^s$
$2^1E$	$0.66(5e \rightarrow 6e)^s - 0.25(3a_1 \rightarrow 6e)^s + 0.66(5e \rightarrow 3a_2)^s$
$3^{1}E$	$-0.61$ (5e $\rightarrow$ 6e ) <sup>S</sup> + 0.72 (5e $\rightarrow$ 3a <sub>2</sub> ) <sup>S</sup>
$4^1E$	$0.92 (3a_1 \rightarrow 8e)^s - 0.36 (2a_1 \rightarrow 8e)^s$
3 <sup>3</sup> A <sub>2</sub>	$0.95(5e \rightarrow 8e)^T$
$5^3E$	$0.96(5e \rightarrow 8e)^T$
$2^{3}A_{1}$	$0.96(5e \rightarrow 8e)^T$
$5^1E$	$0.95 (5e \rightarrow 8e)^s$
$3^{1}A_{2}$	$0.96(5e \rightarrow 8e)^s$
$1^1A_1$	$0.96(5e \rightarrow 8e)^s$
$2^1A_1$	0.83 (5e $\rightarrow$ 6e $)^{s}$ - 0.42 (3a <sub>1</sub> $\rightarrow$ 4a <sub>1</sub> )
$4^{1}A_{2}$	0.96 (5e $\rightarrow$ 7e ) <sup>S</sup>
$6^1E$	$0.79(5e \rightarrow 7e)^5 + 0.56(5e \rightarrow 4a_1)$
$7^1E$	$0.85 (4e \rightarrow 3a_2)^5 + 0.39 (3a_1 \rightarrow 7e)$
$8^1E$	$-0.50 (5e \rightarrow 7e)^s + 0.80 (5e \rightarrow 4a_1) + 0.20 (4e \rightarrow 3a_2)$
$3^{1}A_{1}$	$0.85 (5e \rightarrow 7e)^{s} - 0.52 (3a_1 \rightarrow 4a_1)$
$9^1E$	$0.95 (3a_1 \rightarrow 7e)^5 - 0.43 (4e \rightarrow 3a_2)$
$4^{1}A_{1}$	$0.52 (4e \rightarrow 6e)^5 + 0.34 (5e \rightarrow 7e) + 0.28 (5e \rightarrow 6e)$
$10^{1}E$	$0.96(4e \rightarrow 6e)^s$

Table 8. The lower excited states of  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup>. Configuration mixing<sup>\*</sup>

 $T$  stands for triplet, and S for singlet.

Table 9. Populations for some excited states in  $[Fe(II)-(GMI)_3]^{++}$ 

State	$3d_{-2}$		$3d_{x^2-y^2} + 3d_{xy} 3d_{xz} + 3d_{yz} 4s$		$4p_x + 4p_y 4p_z$		$C(\pi)$	$N(\pi)$	N(n)
Ground <sup>a</sup>	1.947	2.248	1.262	0.424	0.256	0.162	5.139	8.229	10.328
$1^3A_1^b$	0.000	$-0.172$	$-0.081$	0.000	0.018	0.000	$-0.064$	0.302	0.002
$2^1E^b$	$-0.057$	$-0.232$	$-0.108$	0.000	0.012	0.006	0.074	0.301	0.004
$3^{1}E^{b}$	$-0.043$	$-0.242$	$-0.024$	0.000	0.010	0.006	0.036	0.330	0.000
$4^{1}E^{b}$	$-0.881$	0.222	0.553	$-0.002$	0.001	0.000	$-0.074$	$-0.035$	0.217
$5^1E^b$	$-0.001$	$-0.368$	0.518	0.000	0.000	0.000	$-0.270$	$-0.075$	0.196
$4^{1}A_{2}^{b}$	$-0.003$	$-0.379$	$-0.123$	0.000	0.000	0.000	0.389	0.122	0.007 $\overline{\phantom{0}}$
$7^1E^b$	$-0.107$	$-0.042$	$-0.011$	0.001	0.000	0.012	0.380	$-0.231$	0.003 $\equiv$
$8^1E^b$	$-0.004$	$-0.363$	$-0.117$	0.000	0.000	0.001	0.410	0.079	0.006 $\overline{\phantom{0}}$
$9^1E^b$	$-0.526$	$-0.017$	$-0.006$	$-0.001$	0.001	0.003	0.581	$-0.035$	0.001 $\qquad \qquad -$
$5^{1}A_{2}^{b}$	$-0.207$	0.039	0.015	0.005	0.004	0.014	0.362	$-0.205$	0.026 $\equiv$

a Populations.

<sup>b</sup> Change from the ground state population.

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Type		Symmetry Calculated		Observed					
					Present investigation <sup>a</sup>		Hanazaki and	Nagakura <sup>b</sup> [15]	
		$\mathbf{v}$	$\overline{f}$	$v_{\rm max}$	range	$\log \varepsilon_{\rm max}$	ν	$\log \varepsilon$	
$CT + L$	$1^1A_2$	11.2	0.004						
$CT + L$	$1^1E$	13.1	0.03						
<b>CT</b>	$2^1E$	15.9	0.35	19.2		3.86	19.5	3.93	
$CT + d - d$	$3^1E$	17.3	0.003	$20.5^s$	$18 - 23$	3.80	$20.4^s$	3.87	
<b>CT</b>	$2^{1}A_{2}$	22.4	0.003	24.1	$23 - 24.5$	3.18	$24.2^s$	3.38	
$CT+L$	$1^1A_1$	25.6	F						
${\cal C}{\cal T}+L$	$4^1E$	27.7	0.04	$25.5^{s}$	$24.5 - 31$	3.45	$25.6^s$	3.54	
$CT + L$	$3^{1}A_{2}$	28.1	0.29	28.6		3.75	28.74	3.81	
${\cal C}{\cal T}+L$	$5^1E$	29.0	0.20	$29.8^{s}$		3.67			
$CT+L$	$2^1A_1$	31.5	$\boldsymbol{F}$						
$CT + L$	$6^1E$	31.8	0.00004						
$d-d$	$7^1E$	32.8	0.0005						
$CT+L+d-d 8^{1}E$		33.6	0.004						
$CT+L+d-d$ 4 <sup>1</sup> $A_2$		33.8	0.02						
${\cal C}{\cal T}+L$	9 <sup>1</sup> E	33.9	0.10						
$CT + L$	$5^{1}A_{2}$	34.6	0.18						
$CT + L$	$10^1E$	36.7	0.15						
<b>CT</b>	$11^1E$	37.5	0.39	33.4	$32 - 36$	4.77	33.56	4.81	
$CT + L$	$6^{1}A_{2}$	37.9	0.91	$34.5^{\circ}$		4,72	$34.5^s$	4.74	
$CT+L$	$12^{1}E$	40.4	0.02						
${\cal C}{\cal T}+L$	$7^{1}A_{2}$	40.7	0.31			4.22			
$CT + L$	$13^1E$	42.2	0.13	$38.6^{s}$			$38.8^{\rm s}$	4.26	
${\cal C}{\cal T}+L$	$14^1E$	44.4	0.07)		$36 - 43$				
$CT + L$	$8^1A_2$	44.7	0.95	40.5		4.41	40.49	4.44	
$CT + L$	$15^1E$	44.9	0.29	42.0 <sup>s</sup>		4.36	$41.5^s$	4.38	

Table 10. Electronic singlet transitions in  $[Fe(II)-(bipy)_3]^{++}$ . Transition frequencies in kK

The calculations give four singlets with energies lower than  $3<sup>1</sup>E$  and with low intensities.

A shoulder (19.8 kK) is observed on the high energy side of the 18 kK band and is probably due to the vibrational structure. A weak electronic transition,  $4<sup>1</sup>E$ , is predicted to be found in that region. According to the form of the orbitals and the population analysis, the transition to  $4^{1}E$  is a  $d-d$  transition.

The three singlets  $5^{1}E$  (30.9 kK),  $3^{1}A_{2}$  (31.0 kK) and  $1^{1}A_{1}$  (32.3 kK) all have  $(5e \rightarrow 8e)$  as the main configuration, indicating that each of them can be classified as partly  $d \rightarrow d$  and partly CT ( $\pi \rightarrow d + d \rightarrow n$ ) in character, as also shown in Table 9. The calculated weak transitions to  $5^1E$  and  $3^1A_2$  probably correspond to the observed weak band at 29 kK. Transitions to  ${}^{1}A_1$  states are symmetry forbidden. Ito *et al.* [14] did not obtain any transition in this region, probably because  $(d-d)$  transitions were not considered in their method.

Type	Symmetry Calculated			Observed					
					Present investigation <sup>a</sup>	Hanazaki and Nagakura <sup>b</sup> [15]			
		ν	$\int$	$v_{\text{max}}$	range	$\log \varepsilon_{\max}$	ν	$\log \varepsilon$	
L	$16^1E$	47.6	0.07						
L	$17^{1}E$	47.7	0.01						
L	$9^{1}A_{2}$	47.7	0.10						
$CT + L$	$18~{}^1E$	48.1	0.05						
$CT+L$	$10^{1}A_{2}$	48.8	0.11						
L	$19^{1}E$	50.1	0.009						
L	$20^1E$	50.7	0.03						
L	$11^{1}A_{2}$	52.1	0.005						
L	$21~^1E$	52.7	0.31)						
$CT + L$	$22^{1}E$	53.9	0.07						
L	$23^{1}E$	54.1	0.21						
L	$12^{1}A_2$	54.3	1.43	48.3 <sup>s</sup>	$43.5 \rightarrow$	4.84	48 <sup>s</sup>	4.70	
L	$24^{1}E$	55.8	0.83						
L	$25^{1}E$	56.5	0.34						
L	$13^{1}A_{2}$	56.8	0.38						
L	$26^1E$	57.1	0.12						
L	$27^{1}E$	58.0	0.08						

Table 10 (continued)

<sup>a</sup>  $[Fe(bipy)_3] \cdot SO_4 \cdot 5H_2O$  in methanol.

<sup>b</sup>  $[Fe(bipy)_3] \cdot Cl_2 \cdot 7H_2O$  in aqueous solution.

<sup>e</sup> <sup>1</sup>E transitions are polarized perpendicular ( $\perp$ ) to the  $C_3$  axis.

 $^{1}A_{2}$  transitions are polarized parallel (||) with the  $C_{3}$  axis.

 $^{1}A_{1}$  transitions are symmetry forbidden.

s shoulder.

The 4 <sup>1</sup> $A_2$  (48.4 kK) state is a combined CT ( $d \rightarrow \pi^*$ ) and  $L(\pi \rightarrow \pi^*)$  state (Table 9) and may be referred to the observed strong band at 44.3 kK.

Observations indicate a strong UV band at around 54 kK, also observed by Ito *et al.* [14]. It may be assigned to the  $5<sup>1</sup>A<sub>2</sub>$  state that, according to the population analysis, can be classified as partly CT  $(d \rightarrow \pi^*)$  and partly  $L(\pi \rightarrow \pi^*)$ .

In Table 7 the lower calculated triplet and singlet transitions are given together with an estimated range in which to search for the transition. Calculated singlets with fairly safe assignments to observed transitions have been found to be around 2-4 kK too high in energy. The singlet-triplet gap will come out too large from the calculations, by 2–7 kK in the present method [3]. In the region  $10-13 \text{kK}$ we predict two singlet transitions polarized parallel to the threefold z-axis,  $1^1A_2$ and  $2^1A_2$ , and two singlets polarized perpendicular to the threefold z-axis,  $1^1\overline{E}$ and  $2^1E$ . The calculations further predict four low-lying triplets with some CT character,  $1^3A_1$ ,  $1^3E$ ,  $2^3E$  and  $1^3A_2$ .

Type	Symmetry	Calculated		Estimated range, $\nu$ (cf. text)	Observed Present investigation <sup>e</sup>	
		ν	f		$v_{\text{max}}$	$\log \varepsilon_{\rm max}$
$CT + L$	$1^3A_1$	3.3		$5 - 13a$		
$CT + L$	$1^3E$	6.0		$8 - 16^a$	8.85 <sup>d</sup>	0.7
$CT + L$	$1^3A_2$	10.4		$10 - 14^{b}$		
$CT + L$	$1^1A_2$	11.2	0.004	$11 - 14^{b}$		
<b>CT</b>	$2^3E$	11.3		$16 - 19b$	11.8 <sup>d</sup>	0.9
$CT + L$	$1^1E$	13.1	0.03	$13 - 16^{b}$		
CT	$3^3E$	13.5		$15 - 20b$		
CT	$2^1E$	15.9	0.35	$\rightarrow$	19.2	3.86
$CT + d - d$	$3^1E$	17.3	0.003	$\rightarrow$	$20.5^{\rm s}$	3.80
$CT + L$	$2^{3}A_{2}$	18.7		$22 - 24$		
$CT + L$	$4^3E$	20.5		$22 - 28$		
$CT + L$	$3^{3}A_{2}$	21.8		$23 - 28$		
CT	$2^{1}A_{2}$	22.4	0.003	$\rightarrow$	$24.1^s$	3.18

Table 11. The lower electronic singlet and triplet transitions in  $[Fe(II)-(bipy)_3]^+$ . Calculated values and the estimated range in which to search for the transition. Transition frequencies in kK

<sup>a</sup> König and Schläfer [39] assigned a sharp peak at 8.98 kK to a triplet. This peak was later considered by Palmer and Piper [38] as the second overtone of the C-H stretching vibration.

<sup>b</sup> Palmer and Piper [38] observed a weak band located at 11.5 kK and assigned it as a spinforbidden transition  $(3T_1 \leftarrow 1A_1)$ .

<sup>c</sup>  $[Fe(bipy)_3]SO_4 \cdot 5H_2O$  in methanol (10<sup>-4</sup> M).

<sup>d</sup>  $[Fe(bipy)]$ 3 $O_4 \cdot 5H_2O$  in aquaeus solution (0.3 M).

Calculated						Observed [31]	
cis-			trans-		(cyclohexane)		
Symmetry <sup>a</sup>	v		Symmetry <sup>a</sup>	ν		$v_{\rm max}$	$\varepsilon_{\text{max}} \cdot 10^{-4}$
${}^{1}B_{1}(n-\pi^{*})$	36.0			36.5			
$^{1}A_{1}$	39.0	0.02	${}^1\!A_u(n-\pi^*)$ ${}^1\!B_u$	38.8	0.08	35.5	1.50
$B_2$	39.3	0.05	$^{1}A_{g}$	39.4	$\bf{0}$		
$1B_2$	43.5	0.92	${}^1B_u$	43.7	0.99	42.2	1.20
${}^{1}B_{1}(n-\pi^{*})$	47.5		$^{1}A_{u}(n-\pi^{*})$	48.1			
$^{1}A_1$	51.8	0.17	$^{1}A_{q}$	50.4	$\mathbf{0}$		
${}^1B_2$	51.9	0.57	${}^1B_u$	54.1	1.27	52.4	4.0
$^{1}B_{2}$	55.8	0.56	$^{1}A_{g}$	54.5	0		
$^{1}A_{1}$	57.3	0.42	$^{1}A_{g}$	57.4	$\theta$		
$^{1}A_{1}$	57.5	0.79	$^{1}B_{u}$	57.8	1.18		

Table 12. Electronic singlet transition in *cis-* and *trans-forms* of bipyridyl. Transition frequencies in kK

<sup>a</sup> All transitions are  $\pi - \pi^*$  unless otherwise indicated.

## $[Fe(II)–(bipy)_3]^{++}$

The electronic spectra of this complex have been thoroughly investigated experimentally. A review of observed data can be found in three recent articles by König [35], Krumholz [36] and by Bryant, Fergusson and Powell [37]. Characteristic for the observed spectra are two intense bands in the visible at about 19 and 28 kK, and two strong bands in the ultraviolet at about 33 and 40 kK. In the following, these four bands and the region above 40 kK and below 20 kK will be discussed in more detail.

*The Region Around 19 kK.* The intense visible band at around 19 kK has been characterized as a CT band. Its intensity and its structure in crystal spectra [38] excludes a transition of  $d-d$  type. It cannot be a perturbed ligand transition as no band is found for the ligand bipyridyl in that region (cf. Table 12).

The present calculations give only one strong band in this region,  $2^{1}E(15.9 \text{ kK})$ , Table 10), which is a CT ( $d \rightarrow \pi^*$ ) transition, in accord with previous assignments.

The observed shoulder towards higher energy (20.4 kK) has been ascribed to a vibrational structure of the 19 kK band [32, 38]. The calculated  $3^{1}E-2^{1}E$ separation (1.4 kK) indicates that the  $d - \pi^*$  transition to  $3^1E$  is to be found in that region. But as  $3^{1}E$  is predicted to be much weaker than  $2^{1}E$  (the calculated oscillator strength of  $2^1E$  is 0.35 while it is only 0.003 for  $3^1E$ ) it is probably hidden in the absorption spectra.

In between the two strong visible bands we have observed a weak band at 24.1 kK for  $[Fe(bipy)_3] \cdot SO_4 \cdot 5H_2O$  in methanol. Hanazaki and Nagakura [15] report a shoulder at 24.2 kK for  $[Fe(bipy)_3] \cdot Cl_2 \cdot 7H_2O$  in aqueous solution. This band may be assigned to the calculated weak  $2^1A_2$  transition (22.4 kK,  $f=0.003$ ) of  $d \rightarrow \pi^*$  type. For a definite assignment to be made, a more careful analysis of polarization data in the narrow region (23-24.5 kK) remains to be done.

*The Region Around 28 kK.* Like Hanazaki and Nagakura [15] we assign the observed 28.6 kK band to three probably operlapping transitions,  $4^{1}E$  (27.7 kK),  $3<sup>1</sup>A_2$  (28.1 kK) and  $5<sup>1</sup>E$  (29.0 kK) with f-values: 0.04, 0.29 and 0.20 respectively. They can all be classified as partly CT ( $d \rightarrow \pi^*$ ) and partly  $L(\pi \rightarrow \pi^*)$ . As mentioned previously, in the GMI complex the transitions in this region have very low calculated f-values (0.03 and 0.0004) in accord with experimental findings. The difference of intensity for this band in the GMI and the bipyridyl complexes mirrors the fact that the bands are of different character in the two compounds.

The observed shoulder at 25.5 kK is most probably attributed to one of these three transitions, but it is interesting to note that the calculations also give an electronically forbidden transition in that region, to  $1<sup>1</sup>A<sub>1</sub>$  (25.6 kK) characterized as CT  $(d \rightarrow \pi^*) + L(\pi \rightarrow \pi^*)$ .

*The Region Around 33 kK.* The observed strong band at 33.4 kK with a shoulder at 34.5 kK has been assigned to an internal ligand transition [37, 15] shifted to lower energy in comparison with the free ligand. According to the present calculation these bands are clearly due to  $11 ^1E(37.5 kK)$  and  $6^1A_2(37.9 kK)$ . Calculations for planar bipyridyl *(trans),* with the same carbon and nitrogen parameters as used in the present study, give the lowest  $\pi - \pi^*$  transition at 38.8 kK (Table 12). The MO calculation of the iron complex thus gives two transitions "shifted" to lower energy compared with the lowest  $\pi - \pi^*$  transition of bipyridyl. But 11<sup>1</sup>E and  $6<sup>1</sup>A<sub>2</sub>$  cannot be classified as internal ligand transitions. They both have some  $d-\pi^*$  character, transferring 0.70 resp. 0.36 electrons from iron d orbitals to the ligand  $\pi$  system.

*The Region Around 40 kK.* The observed band at 40.5 kK, with a shoulder on the low energy side at 38.6 kK and a shoulder on the high energy side at 42.0 kK has previously been considered as due to the second  $\pi - \pi^*$  transition in bipyridyl [37]. In this region the present calculation gives one strong transition,  $8^1A_2$ , surrounded by two weaker transitions,  $14^{1}E$  and  $15^{1}E$ . The low energy shoulder may be assigned to  $7^1A_2$  and  $13^1E$ . All of these five states can be classified as CT  $(d \rightarrow \pi^*)$  +  $L(\pi \rightarrow \pi^*)$  states with an electron transfer of about 0.3–0.4.

The Region in Far UV. Observations have not been extended further than 48 kK. They show a region with increasing intensity from 43.5 kK (Table 10). The calculations give two strong transitions,  $12^{1}A_2$  (54.3 kK) and  $24^{1}E$  (55.8 kK), classified as transitions within the  $\pi$ -system of the bipyridyl molecules. The calculated spectral pattern for  $[Fe(II)-(bipy)_3]^{++}$  in this region resembles the one for *cis-bipyridyl*, as can be seen from Tables 10 and 12. For bipyridyl in cyclohexane solution there is an observed strong band at 52.4 kK (Table 12).

*The Region Below 20 kK.* The lower singlet and triplet transitions are given in Table 1t. Palmer and Piper [38] observed in crystal spectra a weak band at 11.5 kK polarized perpendicular to the threefold z-axis. They assigned it as a spinforbidden  $d-d$  transition  $({}^1A_1-{}^3T_1$  in  $O_h$ ) gaining intensity through spinorbit coupling with the visible CT band around 19 kK. They further attributed a weak sharp peak at 8.89 kK to the second overtone of the C-H stretching vibration. König and Schläfer [39] made a different assignment of the corresponding peak at 8.98 kK in solution spectra. They considered it to be a  $^{1}A_{1} - ^{3}T_{1}(O_{h})d-d$ transition. According to the present calculation there are no *d-d* singlets or triplets in this low energy region. The observed band at 11.5 kK in crystal spectra [38] and 11.8 kK in solution spectra (Table 11) can most probably be assigned to the weak perpendicularly polarized  $1^1E$  transition. According to the present calculations the tail of the observed strong band at 19.2 kK may be constituted of two weak singlets,  $1^1E$  and  $1^1A_2$ , and three triplets,  $1^3A_2$ ,  $2^3E$  and  $3^3E$ .

Two low-lying triplets,  $1^3A_1$  and  $1^3E$ , are predicted. Both or one of them may be attributed to the 8.85 kK peak, but it should be stressed that as yet there exist no clear experimental evidence for them. They might be revealed in luminescence spectra or by the aid of ESR measurements.

### **8. Conclusions**

The method used in the present calculations had previously been applied in studies of organic copper complexes [4-7] and proven to be capable of giving a quantitative account for many different properties depending on the electronic structure. The present investigation shows that the method is also well suited for studies of iron organic compounds. The scheme for evaluation of one-center iron parameters and parameters describing the iron-ligand bond can of course be extended to other transition elements.

The results can be summarized as follows: For both  $[Fe(II)-(GMI)<sub>3</sub>]$ <sup>++</sup> and  $[Fe(II) - (bipy)_3]^{++}$  the calculated electronic population of the iron is in accord with Mössbauer isomer shift data, indicating that a realistic electron distribution has been obtained for the normal state. The electronic spectra of both compounds are quantitatively analyzed. Ligand field, charge transfer, and intraligand transitions are treated simultaneously and the interaction between them is properly taken into account. The method makes it possible to explain detailed properties of the electronic spectra, e.g. the difference in intensity for the visible band in the neighbourhood of 29 kK in the two similar compounds.

Previous assignments based on  $O<sub>h</sub>$  symmetry and crystal field theory can only be expected to give a rough qualitative picture of the spectral pattern, as trigonal distortion and covalency have been neglected. It is thus not astonishing that the present assignments for some bands differ considerably from previous conventional assignments.

For both compounds triplet  $[CT(d \rightarrow \pi^*)+L(\pi-\pi^*)]$  states are predicted to be found in the near IR. The experimental verification of these bands remains to be done.

### **Appendix**

## *One-Center Parameters for lron from Observed Atomic Spectra and Atomic Analytical Hartree-Fock Wave Functions*

In a semiempirical method considering the valence electrons  $(3d, 4s \text{ and } 4p)$ of the transition metal ion, it would be desirable to obtain from experimental data the numerical values of the metal one-center parameters for different electronic populations and charges of the ion. Atomic spectral data can be used for the determination of the two-electron Slater-Condon parameters,  $F_k(\mu, v)$ ,  $G_k(\mu, v)$ , and the one-electron parameters  $\varepsilon_n$  (Eq. 6, Section 4). This is so because the energy of a spectroscopic term of an atom can be expressed in terms of these parameters  $[40-42]$ . With the assumption of a "frozen core" the energy is given by the expression:

$$
E^{i,q} = C + \sum_{\mu} a^q(\mu) \varepsilon_{\mu} + \sum_{\mu > \nu} \left\{ b^q(\mu, v) F_0(\mu, v) + \sum_{k \neq 0} \left[ c_k^{i,q}(\mu, v) F_k(\mu, v) - d_k^{i,q}(\mu, v) G_k(\mu, v) \right] \right\}
$$
(15)

where C is a constant particular to the element,  $\mu$  and  $\nu$  denote atomic valence orbitals, and i detones the  $i<sup>th</sup>$  term of the configuration g.

Hinze and Jaffé [42] in an extensive study of the first transition elements using atomic term energies determined the Slater-Condon parameters with  $k \neq 0$  for the neutral atom and the monopositive ion. Later Tondello *et al.* [-43] using certain theoretical conditions together with spectral data made a new determination of the Slater-Condon parameters  $(k+0)$  assuming the parameters to be charge dependent. Because of the lack of enough experimental information, it will not be possible to deduce from observed data only, the charge and configuration dependence of all one-center parameters needed in semiempirical calculations. Some extra assumptions have to be made.

In the present work a procedure for obtaining  $F_k(\mu, v)$ ,  $G_k(\mu, v)$  (including  $k = 0$ ) and  $\varepsilon_u$  for iron is presented. Atomic spectral data [44] are used in combination with some relations between theoretical Slater-Condon parameters, obtained from atomic analytical Hartree-Fock wave functions [25, 26, 45]. Recently a different approach was given by Anno and Teruya [46] in an elaborate study of the Slater-Condon parameters of all first transition elements.

The experimental spectroscopic energy of a multiplet was determined from Moore's tables [44] as a weighted mean of the  $J$  states. The following configurations and multiplets were considered.

$$
d^{8} : {}^{3}F
$$
\n
$$
d^{7} s : {}^{5}F, {}^{5}P, {}^{3}H, {}^{1}H, {}^{3}G, {}^{1}G
$$
\n
$$
d^{6} s^{2} : {}^{5}D, {}^{3}H, {}^{3}G, {}^{3}D, {}^{1}I
$$
\n
$$
d^{7} p : {}^{5}F, {}^{5}G, {}^{5}S, {}^{5}P, {}^{3}I, {}^{1}I
$$
\n
$$
d^{6} s p : {}^{7}D, {}^{7}F, {}^{7}P
$$
\n
$$
d^{7} : {}^{4}F, {}^{4}P, {}^{2}G, {}^{2}H, {}^{2}F
$$
\n
$$
d^{6} s : {}^{6}D, {}^{4}H, {}^{4}G, {}^{2}H, {}^{2}I
$$
\n
$$
d^{5} s^{2} : {}^{6}S, {}^{4}D
$$
\n
$$
d^{6} p : {}^{6}D, {}^{6}F, {}^{6}P, {}^{4}I, {}^{2}K
$$
\n
$$
d^{5} s p : {}^{8}P
$$
\n
$$
d^{6} : {}^{5}D, {}^{3}H, {}^{3}G, {}^{3}D, {}^{1}I, {}^{3}\overline{F}, {}^{1}F, {}^{1}\overline{G}
$$
\n
$$
d^{5} s : {}^{7}S, {}^{5}S, {}^{5}G, {}^{5}D, {}^{5}F, {}^{3}H, {}^{1}H
$$
\n
$$
d^{5} p : {}^{7}P, {}^{5}H, {}^{3}K, {}^{1}K.
$$

For  ${}^{3}\overline{F}$  and  ${}^{1}\overline{G}$  in the configuration  $d^{6}$ , an average over two multiplets was used.

## $F_k(\mu, \nu)$  and  $G_k(\mu, \nu)$  for  $k \neq 0$

The parameters  $F_2(d, d)$ ,  $F_4(d, d)$  and  $G_2(s, d)$  were determined in the classical manner by a least-squares procedure from term energies for each considered configuration not containing 4p. Different values for different configurations were obtained. An analysis of these values shows that  $F_2(d, d)$  and  $F_4(d, d)$  depend strongly and almost linearly on the number of 3d-electrons  $(n_{3d})$  and weakly on  $n_{4s}$ . Thus  $F_2(d, d)$  and  $F_4(d, d)$  are assumed to be linear functions of  $n_{3d}$  and a leastsquares procedure gives:

$$
F_2(d, d) = 1.418 - 0.171 (n_{3d} - 6) \text{ in kK},\tag{16}
$$

$$
F_4(d, d) = 0.114 - 0.009 (n_{3d} - 6) \text{ in kK} \tag{17}
$$

It is also reasonable to describe  $G_2(s, d)$  as a linear function of the charge, q.

$$
G_2(s, d) = 1.290 + 0.269 q \text{ in kK}.
$$
 (18)

The values of  $F_2(d, d)$ ,  $F_4(d, d)$  and  $G_2(s, d)$  determined from Eqs. (16), (17) and (18) were then used in the expressions for the term energies in configurations with  $4p$ . Different values of  $F_2(p, d)$  and  $G_3(p, d)$  for different configurations were obtained. (No value of  $F_2(p, d)$  could be determined for  $d^5 p$ .)

 $G_3(p, d)$  can be described as a linear function of q:

$$
G_3(p, d) = 0.0162 + 0.0077 q \text{ in kK} \tag{19}
$$

As there are not enough experimental spectroscopic data to allow for an analysis of the configuration dependence of  $F_2(p, d)$ , a comparison was made with theoretical values of this parameter. The theoretical data indicates that  $F_2(p, d)$  is nonlinearly q-dependent. In Table 1 the values of  $F_2(p, d)$  for  $q = 0$  and  $q = 1$  are the experimentally derived values; the value for  $q = 2$  is a "scaled" theoretical value,

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where the scaling factor is the average quotient between experimental and theoretical values for  $q = 0$  and 1.

As  $G_1(p, d)$  could not be determined from the observed term energies, used in the present investigation, the values of this parameter are determined as:

$$
G_1^e(p, d) = \left[\frac{G_1^t(p, d)}{G_3^t(p, d)}\right]_{\text{average value}} \cdot G_3^e(p, d)
$$
 (20)

where the index  $e$  stands for experimental and  $t$  for theoretical. As the quotient between  $G^t_1(p, d)$  and  $G^t_3(p, d)$  is found to be almost constant for different configurations, an average value of the quotient is used. It was not possible to determine  $G<sub>1</sub>(s, p)$  from the term energies considered, as it always occurs in the combination:

$$
F'_{0}(s, p) = [F_{0}(s, p) - G_{1}(s, p)].
$$
\n(21)

## $\varepsilon_u$  and  $F_0(\mu, \nu)$

The parameters  $\varepsilon_{\mu}$  and  $F_0(\mu, v)$  ( $F'_0(s, p)$  replacing  $F_0(s, p)$ ) cannot be determined from term energies of just one configuration. "Average" values, over different ionic states and configurations, for these parameters, were derived from expressions of the barycenter energies of each configuration considered.

The values of  $F_k(\mu, v)$  and  $G_k(\mu, v)$  for  $k \neq 0$ , derived in the manner described above, were inserted in the expressions for the barycenter energies, giving linear equations for  $\varepsilon_u$  and  $F_0(\mu, v)$ . The "average" values,  $\bar{\varepsilon}_u$  and  $\bar{F}_0(\mu, v)$  were determined from a least-squares fit to the equations thus obtained.

Theoretical values of  $F_0^t(\mu, v)$  were calculated and corresponding average values,  $\overline{F}_0^t(\mu, v)$  derived. An analysis of theoretical  $F_0^t(\mu, v)$  values was made. It turned out that  $F_0^t(d, d)$  with rather good accuracy can be described as a linear function of  $n_{3d}$ , while  $F_0^t(s, s)$ ,  $F_0^t(s, p)$ ,  $F_0^t(s, d)$  and  $F_0^t(p, d)$  can be considered as nonlinear functions of q. This simplified population dependence of the theoretical  $F_0^t$  values is transformed to the semiempirical parameters by the formula:

$$
F_0^e(\mu, \nu) = \left[ \frac{\overline{F}_0^e(\mu, \nu)}{\overline{F}_0^t(\mu, \nu)} \right] \cdot F_0^t(\mu, \nu) \,. \tag{22}
$$

The obtained values of  $F_0^e(\mu, \nu)$  (see Table 1) were then inserted in the expressions for the barycenter energies of each configuration, giving linear equations for  $\varepsilon_{\mu}$ . These equations can be solved assuming  $\varepsilon_{3d}$  to be a function of  $n_{3d}$ , and  $\varepsilon_{4s}$  and  $\varepsilon_{4p}$ to be functions of q. These assumptions are in line with the results for  $F_k(\mu, \nu)$ . The obtained semiempirical values of the one-center parameters are presented in Table 1. The values of  $G_f^e(s, p)$  and  $F_0^e(s, p)$ , given in Table 1, are obtained from the values of  $F_0^e(s, p)$  assuming  $[G_1^e(s, p)/F_0^e(s, p)]$  equal to the average theoretical value of  $[G_1^t(s, p)/F_0^t(s, p)]$ .  $F_0(p, p)$  and  $F_2(p, p)$  cannot be derived from experimental data. The values given in Table 1 have been roughly estimated as:

$$
F_0^e(p, p) = 2F_0^e(s, p) - F_0^e(s, s) ,
$$
\n(23)

$$
F_2^e(p, p) = \left[\frac{F_2^t(p, p)}{F_0^t(p, p)}\right]_{\text{average value}} \cdot F_0^e(p, p) \,. \tag{24}
$$

**The semiempirical parameters obtained are found to reproduce the spectroscopic energy terms of Fe in different ionic states with a standard deviation of 1.63 kK.** 

**The present procedure can be considered as a method to "scale" theoretical parameter values in those cases where a direct determination from experimental data is not possible. The values in Table 1 must be looked upon as "a first trial" to these important parameters. New experimental data in combination with wave functions accounting for correlation (and eventually relativistic effects) will probably allow for a more detailed description of the configuration dependence of the parameters. A similar procedure can of course be used in a systematic study of all transition elements.** 

*Acknowledgement.* This investigation has been supported by grants from the Swedish Natural Science Research Council. The authors wish to express gratitude to Prof. Inga Fischer-Hjalmars for her encouraging interest throughout the work and also to Dr. Björn Roos for valuable discussions. Thanks are also due to Mr. Lars Norén for assistance in numerical computations.

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Dr. M. Sundbom Institute of Theoretical Physics University of Stockholm Vanadisvägen 9 113 46, Stockholm, Sweden